Exploring the Parameter Space of Cosmic-Ray Propagation with Machine Learning



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Introduction

- Context: Study of cosmic-propagation based on the measured nuclei spectra
- Motivation: Suitable propagation conditions needed to use electron/positron cosmic rays for studying astrophysical sources and dark matter signatures.
- Hypothesis: Structures/differences in nuclei spectra caused by propagation

 \rightarrow Goal: Find propagation conditions explaining the current nuclei spectra measurements assuming a common source spectrum for all primary nuclei

Model and Calculation Method

- Common source spectrum: power law with index γ_l below, and γ_h above the break at R_{bi} with softness s_{bi} , and with an exponential cut-off at R_{cut}
- Diffusion coefficient depending on position and with two breaks in rigidity dependence:

$$D(r, z, D) = D_0 \max\left(e^{(r-r_n)/r_s}, 1\right) \max\left(e^{(z-z_n)/z_s}, 1\right) \left(\frac{R}{4 GV}\right)^{\delta_l} \left(1 + \left(\frac{R}{R_{bl}}\right)^{\frac{\delta-\delta_l}{s_l}}\right)^{s_l} \left(1 + \left(\frac{R}{R_{bh}}\right)^{\frac{\delta-\delta_h}{s_h}}\right)^{-s_l}$$

- Diffusive re-acceleration with Alven speed v_a and convection with speed v_c
- Calculations done with DRAGON [D. Gaggero et al., Phys.Rev.Lett. 111(2), 021102 (2013)]
- Modifications: Soft breaks in source spectrum and diffusion coefficient function, double exponential spatial dependence of the diffusion coefficient

18-Dimensional Parameter Space

Sources	Low rigidity index	Break rigidity	Break softness	High rigididty index	Cut-off rigidity	Spiral arm width
	Υ _I	R_{bi}	S _{bi}	Υ _h	R_{cut}	W _{sa}
Diffusion	Diffusion coefficient normalization	Radial scale distance	Exponential scale height	Low rigidity index	Low break rigidity	Low break softness
	D ₀	r _s	Z _s	δ _ι	R _{bl}	S
	Mid rigidity index	High break rigidity	High break softness	High rigidity index	Alven velocity	Convection Velocity
	δ	R_{bh}	S _h	δ_{h}	V _a	Vc

Previous Best-fit Model



Impact of new Helium Data

CALET Helium data [Phys. Rev. Lett. 130, 171002 (2023)] shows a steeper hardening than in the proton spectrum → harder spectrum in conflict with TeV proton data (already upper side of errors) \rightarrow challenge to the assumption of a common injection spectrum

 \rightarrow search parameter space w. convection if there is a solution



Optimizing DRAGON Parameters

- Model quality parameters extracted from fit of normalization and solar modulation parameters to data. Examples:
 - Total χ^2 of all experimental data
 - $\rightarrow\,$ not suitable, experiments with many data-points dominate
 - Likelihood (p-value of single exp.), neg. log. sum over experiments (Sum-NLL)
 - \rightarrow all experiments have equal weight
 - Negative log of p-value for single worst fitting experiment (Max-NLL)
 → best to see if model can agree to each experiment, but not smooth function
- Parameter space so far probed by "random" walk, combination of different methods used to select next model to calculate. Examples:
 - randomly within a given step size
 - by interpolating/extrapolating parameters of already calculated models
- Calculation of full Nickel-proton spallation network very time consuming

 → to test if Helium-Proton hardening discrepancy can be solved,
 calculating helium-proton (with antiproton) range is sufficient

New Approach

- Try to predict the likelihood as a function of the input parameters to have a better chance of finding better parameters in each optimization step.
 - \rightarrow 18 dimensional parameter space \rightarrow Machine Learning
- Investigated methods:
 - Neural Network (promising but difficult to set up, over-training)
 - Bayesian Optimization (for coarsely exploring parameter space)
 - Focus of this talk: Gradient Descent on Ridge Model

Method

• Fit a **ridge model** (regularized polynomial function) to the (preprocessed) likelihood (*Y*) results, parameters are the (preprocessed) DRAGON input parameters (*X*)



 Hyper-parameters (polynomial degree, regularization parameter) are determined by splitting the existing data in training (90%) and test (10%) samples and optimizing for best prediction of the test samples by the model

(polynomial terms are all combinations of the parameters with combined power of the polynomial's degree: 1329 for 18 parameters and 3rd degree)

- Determine gradient of function at a start-point (best likelihood or random) and take a step in negative gradient direction
 - \rightarrow new set of parameters to be calculated by DRAGON
- Using tools from the scikit-learn library

Parameter Space

scatter plots of the already calculated points with pairs of parameters as axes



High energy diffusion coefficient power law index fixed to 0.0001 (equivalent to 0) since optimization converged to this lower boundary

Parameter Space

2.96 0.16 34 2.95 0.14 0.12 2.94 B 0.10 R_{bi} 5 2.93 2 0.08 28 2.92 0.06 26 2.91 0.04 24 0.02 2.05 2.06 2.07 2.08 2.09 2.10 2.11 2.12 010 0.12 014 016 0.18 0,20 0 22 20 29 22 33 R_{cut} S_{bi} V 12.8 -0.56 12.6 0.55 6.0 12.4 0.54 12.2 5.5 0.53 R_{bl} N 3 12 (0.52 5.0 0.51 11.6 4 5 0.50 11.4 11.2 0.49 7.4 8.4 8.6 3.0 3.2 3.4 3.6 3.8 0.12 0.13 0.14 0.15 0.16 0.17 0.18 0.19 76 7 8 8.2 4.0 Do δ 0.38 0.000104 30 0.36 25 0.000102 0.34 20 Sh V_{c} 54 0.000100 15 0.32 0.000098 10 0.30 0.000096 0.07 0.08 0.09 0.10 0.11 0.12 450 475 500 525 550 575 600 625 650 17.0 17.5 18.0 18.5 19.0 19 5 20.0 20.5 0.06 R_{bh} Va S

Take diffusion coefficient normalization vs. power law index as an example to demonstrate data pre-processing



Step 1: subtract mean and scale to variance (sklearn.preprocessing. StandardScaler)



Step 1:

subtract mean and scale to variance (sklearn.preprocessing. StandardScaler)

 → this allows for calculating distances
 between models using an Euclidean metric
 → used for weighting of points in fitting of the ridge model



Step 2: subtract position of the start point (best point)



Step 2: subtract position of the start point (best point)

→ the intercept of the polynomial function is set to zero
 → likelihood is also scaled and shifted
 → the start point
 becomes the origin and the function is forced to be correct there





Weighting in Ridge Model Fit



No Weights:

All points are considered equally in the fitting

Weighting in Ridge Model Fit



Distance Weights:

We are most interested in the function being correct near the start point \rightarrow weight reduced with distance from start point



Weighting in Ridge Model Fit



Exponential Weights:

We are most interested in the function being correct for points with good likelihood (reduce influence of outliers with very high neg. log. likelihood)

$$w = e^{-NLL}$$

Gradient Steps

- Gradient is calculated numerically by finite steps in each parameter direction
- Distance Δ to go in direction of negative gradient is calculated by evaluating the polynomial function along the gradient axis and finding the minium.
- A pre-set maximum distance Δ_{max} is taken if no minimum found.



• After performing the DRAGON calculation at the new point and obtaining a likelihood value, it is added to the point sample and it becomes the start-point for the next step

Preliminary Results (Sum-NLL)



Preliminary Results (Sum-NLL)



Preliminary Results (Max-NLL)



Preliminary Results (Max-NLL)



Current Best Fit Model



minimum p-value is 0.04 \rightarrow 96 %CL exclusion \rightarrow progress, but need further improvement

Conclusions / Outlook

- The ridge model gradient descent algorithm is a first implementation of a machine learning algorithm to understand the parameter space of cosmic ray propagation and support the numerical calculation with DRAGON.
- The stronger hardening of the Helium spectrum compared to proton is difficult to explain with a common injection spectrum, but the found best-fit model suggests an explanation based on propagation effects may be possible.
- Further evaluation and tuning of the algorithm ongoing.
- Next goal: Prediction of likelihood by neural network aiming for better performance also with not smooth loss functions (i.e. Max-NLL).

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Backup Slides

Hypothesis: Differences in Nuclei Spectra Caused by Propagation

- Observed spectra are power laws but the index changes with rigidity at several points: (1) Softening @ O 10 GV,
 (2) Hardening @ O 100 GV 1 TV, (3) Softening @ O 10 TV
- Indices and break positions different between proton and He (and other nuclei, but less significant)
- Possible Explanations:
 - Source spectrum different for each nuclei species
 - Propagation causes differences in spectral shape

 \rightarrow Assumed common source spectrum: power law with index γ_l below, and γ_h above the break at $R_{_{bi}}$ with softness $s_{_{bi}}$, and with an exponential cut-off at $R_{_{cut}}$



Diffusion Coefficient Structure

- Further spectral changes of the nuclei spectra are modeled by two breaks in the rigidity dependence of the diffusion coefficient, softening from δ_{I} to δ at R_{hI} with softness s_{I} , then hardening again to δ_{h} at R_{hh} with softness s_{h}
- Diffusion coefficient depends on position exponential increase with galactic radius r, distance from galactic plane z constant central zones: galactic center $r_n = 2$ kpc, galactic disc $z_n = 0.15$ kpc

$$D(r, z, D) = D_0 \max\left(e^{(r-r_n)/r_s}, 1\right) \max\left(e^{(z-z_n)/z_s}, 1\right) \left(\frac{R}{4 GV}\right)^{\delta_l} \left(1 + \left(\frac{R}{R_{bl}}\right)^{\frac{\delta-\delta_l}{s_l}}\right)^{s_l} \left(1 + \left(\frac{R}{R_{bh}}\right)^{\frac{\delta-\delta_h}{s_h}}\right)^{-s_h}$$

 Motivation: Sources concentrated in galactic center and disk cause magnetic field turbulence, influence decreasing with distance – different propagation conditions for nuclei species depending on how far they propagate out into the halo and back based on nuclei mass and A/Z

Experimental Data Used (Spectra)

Proton Flux

- 0.13 0.35 GeV: Voyager APJ 831(1), 18 (2016)
- 5 GeV 1 TeV: AMS-02 PRL 114, 171103 (2015)
- 1 60 TeV : CALET PRL 129, 101102 (2022)

• Helium Flux

0.11 – 0.66 GeV: Voyager APJ 831(1), 18 (2016) 11 GV – 643 GV: AMS-02 PRL 115, 211101 (2015) 1 TeV – 250 TeV: CALET PRL 130, 171002 (2023)

Carbon & Oxygen Flux
 10 GeV – 2.2 TeV: CALET PRL 125, 251102 (2020)



Using data above 5 GeV/nucleon or equivalent rigidity – solar modulation difficult to model below this energy → Voyager data for lower energy range



Experimental Data Used (Ratios)

- Antiproton fraction
- 5 450 GV: AMS-02 PRL 117, 091103 (2016)
- ³He/⁴He ratio
- 5 10 GeV: AMS-02 PRL 123, 181102 (2019)
- B/C ratio

5 GeV - 1.3 TeV: AMS-02 PRL 117, 231102 (2016)

• ⁷Be/Be ratio

0.25 - 0.85 GeV: PAMELA Universe 7 (2021) 6, 183

• ¹⁰Be/⁹Be ratio

0.25 – 0.85 GeV: PAMELA Universe 7 (2021) 6, 183



Thickness: A "Data-Driven" Approach, Francesco Nozzoli, Cinzia Cernetti

Fitting the Spectra to the Data

- Parameters fitted by minimizing total χ^2 of all experimental data
 - Normalization correction factors
 - Proton
 - Helium
 - Carbon
 - Oxygen
 - Solar modulation potential parameters



- Φ₀
- Φ_{1+} (positive charge)
- Φ_{1-} (negative charge)

$$\Phi = \Phi_0 + \Phi_{1\pm} \left(\frac{1 + (R/R_0)^2}{((R/R_0)^3)} \right)$$

solar modulation potential:

Charge sign and rigidity dependent

based on

Ilias Cholis, Dan Hooper, Tim Linden Phys. Rev. D 93, 043016 (2016) "A Predictive Analytic Model for the Solar Modulation of Cosmic Rays"

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