

# A Model for Propagation of Cosmic Rays from Nuclei Spectra Measurements

JPS autumn meeting  
Okayama, 2022/8/6

6aA124-13



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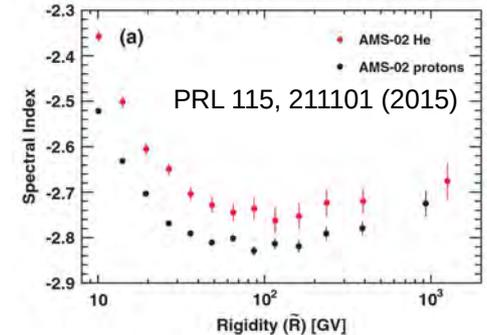
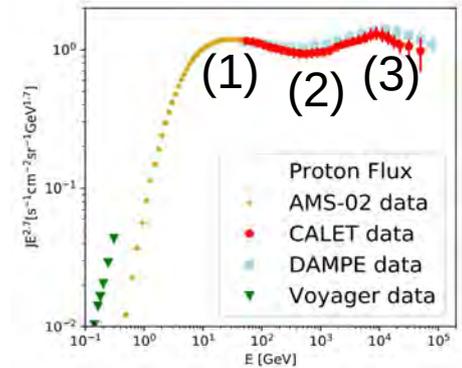
# Introduction

- Motivation: Suitable propagation conditions needed to use electron/positron cosmic rays for studying individual astrophysical sources (nearby SNR) and indirect search for dark matter signatures.
- Nuclei cosmic rays experience much less energy loss than electrons
  - Longer propagation distances and times
  - Sources distributed throughout the galaxy and over millions of years
  - $\sim 3$  SN/100 yr: individual source positions and ages less important for observed nuclei spectra at Earth
- Relations between **nuclei spectra can reveal propagation conditions**:
  - Production of secondary cosmic rays depends on amount of ISM encountered
  - Unstable nuclei and their decay products depend on the residence time

**Goal: Find propagation conditions explaining the current nuclei spectra measurements assuming a common source spectrum for all primary nuclei**

# Hypothesis: Differences in Nuclei Spectra Caused by Propagation

- Observed spectra are power laws but the index changes with rigidity at several points: (1) Softening @  $\sim 10$  GV, (2) Hardening @  $\sim 100$  GV – 1 TV, (3) Softening @  $\sim 10$  TV
- Indices and break positions different between proton and He (and other nuclei, but less significant)
- Possible Explanations:
  - Source spectrum different for each nuclei species
  - **Propagation causes differences in spectral shape**



→ Assumed common source spectrum: power law with index  $\gamma_l$  below, and  $\gamma_h$  above the break at  $R_{bi}$  with softness  $s_{bi}$ , and with an exponential cut-off at  $R_{cut}$

# Diffusion Coefficient Structure

- Further spectral changes of the nuclei spectra are modeled by **two breaks in the rigidity dependence of the diffusion coefficient**, softening from  $\delta_l$  to  $\delta$  at  $R_{bl}$  with softness  $s_l$ , then hardening again to  $\delta_h$  at  $R_{bh}$  with softness  $s_h$
- **Diffusion coefficient depends on position** – exponential increase with galactic radius  $r$ , distance from galactic plane  $z$  – constant central zones: galactic center  $r_n = 2$  kpc, galactic disc  $z_n = 0.15$  kpc

$$D(r, z, D) = D_0 \max\left(e^{(r-r_n)/r_s}, 1\right) \max\left(e^{(z-z_n)/z_s}, 1\right) \left(\frac{R}{4GV}\right)^{\delta_l} \left(1 + \left(\frac{R}{R_{bl}}\right)^{\frac{\delta_l - \delta}{s_l}}\right)^{-s_l} \left(1 + \left(\frac{R}{R_{bh}}\right)^{\frac{\delta - \delta_h}{s_h}}\right)^{-s_h}$$

- Motivation: Sources concentrated in galactic center and disk cause magnetic field turbulence, influence decreasing with distance – **different propagation conditions for nuclei species** depending on how far they propagate out into the halo and back based on nuclei mass and  $A/Z$

# Used Tool: DRAGON

- Publicly available program for numerical calculation of CR propagation on grid in space and momentum D. Gaggero et al., Phys.Rev.Lett. 111(2), 021102 (2013)
- Important features:
  - Spiral arm structure of source distribution & gas
  - Non-equidistant grid in space – 0.5 kpc in halo reduced to 0.05 kpc near galactic plane to allow for gradual diffusion coefficient change
- Own modifications:
  - Soft breaks in source spectrum and diffusion coefficient function
  - Double exponential spatial dependence of the diffusion coefficient

# The Parameter Space

<b>Sources</b>	Low rigidity index	Break rigidity	Break softness	High rigidity index	Cut-off rigidity	Spiral arm width
	$Y_l$	$R_{bi}$	$S_{bi}$	$Y_h$	$R_{cut}$	$W_{sa}$
<b>Diffusion</b>	Diffusion coefficient normalization	Radial scale distance	Exponential scale height	Low rigidity index	Low break rigidity	Low break softness
	$D_0$	$r_s$	$z_s$	$\delta_l$	$R_{bl}$	$S_l$
	Mid rigidity index	High break rigidity	High break softness	High rigidity index	Alven velocity	<b>17 free parameters in total</b>
	$\delta$	$R_{bh}$	$S_h$	$\delta_h$	$v_a$	

# Experimental Data Used (Spectra)

- **Proton Flux**

0.13 – 0.35 GeV: Voyager APJ 831(1), 18 (2016)

5 GeV – 1 TeV: AMS-02 PRL 114, 171103 (2015)

1 – 60 TeV : CALET PRL 129, 101102 (2022)

- **Helium Flux**

0.11 – 0.66 GeV: Voyager APJ 831(1), 18 (2016)

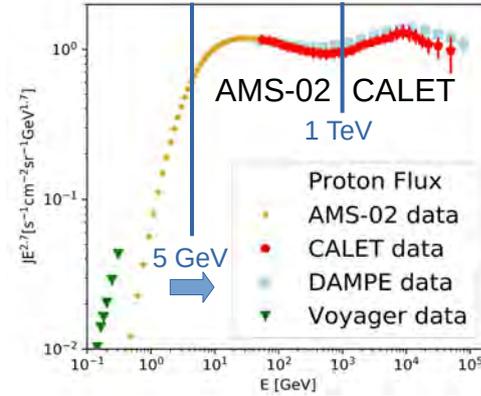
11 GV – 3 TV: AMS-02 PRL 115, 211101 (2015)

- **Carbon Flux**

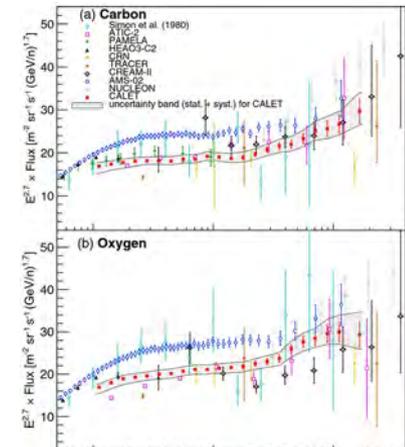
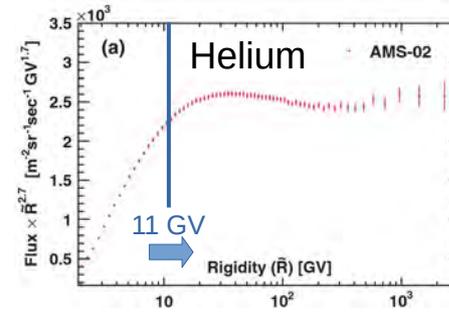
10 GeV – 2.2 TeV: CALET PRL 125, 251102 (2020)

- **Oxygen Flux**

10 GeV – 2.2 TeV: CALET PRL 125, 251102 (2020)



Using data above 5 GeV/nucleon or equivalent rigidity – solar modulation difficult to model below this energy → Voyager data for lower energy range



# Experimental Data Used (Ratios)

- **Antiproton fraction**

5 – 450 GV: AMS-02 PRL 117, 091103 (2016)

- **$^3\text{He}/^4\text{He}$  ratio**

5 – 10 GeV: AMS-02 PRL 123, 181102 (2019)

- **B/C ratio**

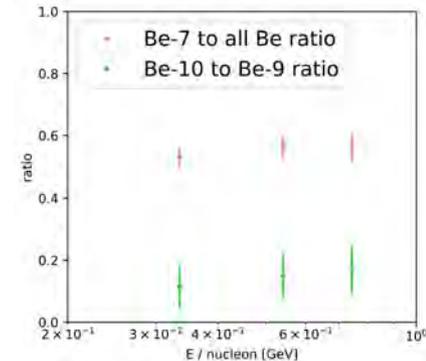
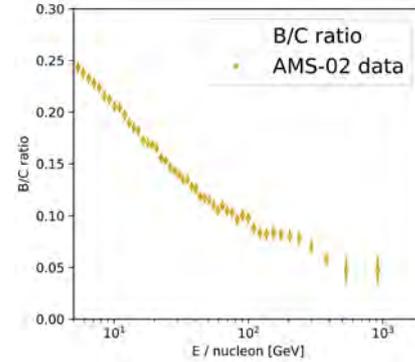
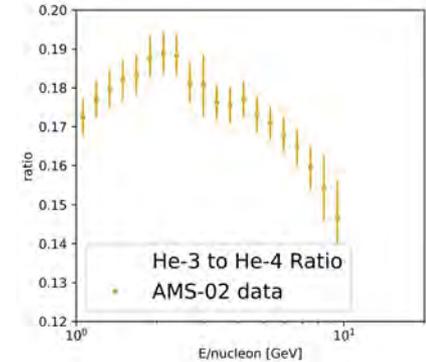
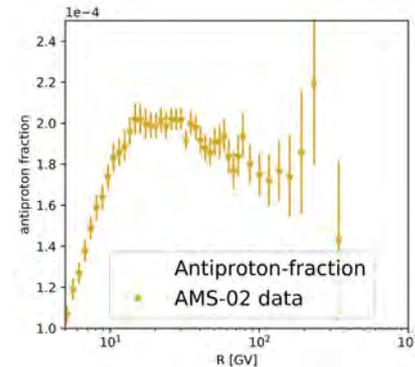
5 GeV – 1.3 TeV: AMS-02 PRL 117, 231102 (2016)

- **$^7\text{Be}/\text{Be}$  ratio**

0.25 – 0.85 GeV: PAMELA Universe 7 (2021) 6, 183

- **$^{10}\text{Be}/^9\text{Be}$  ratio**

0.25 – 0.85 GeV: PAMELA Universe 7 (2021) 6, 183



Universe 7 (2021) 6, 183  
Beryllium Radioactive Isotopes as a  
Probe to Measure the Residence Time  
of Cosmic Rays in the Galaxy and Halo  
Thickness: A “Data-Driven” Approach,  
Francesco Nozzoli, Cinzia Cernetti

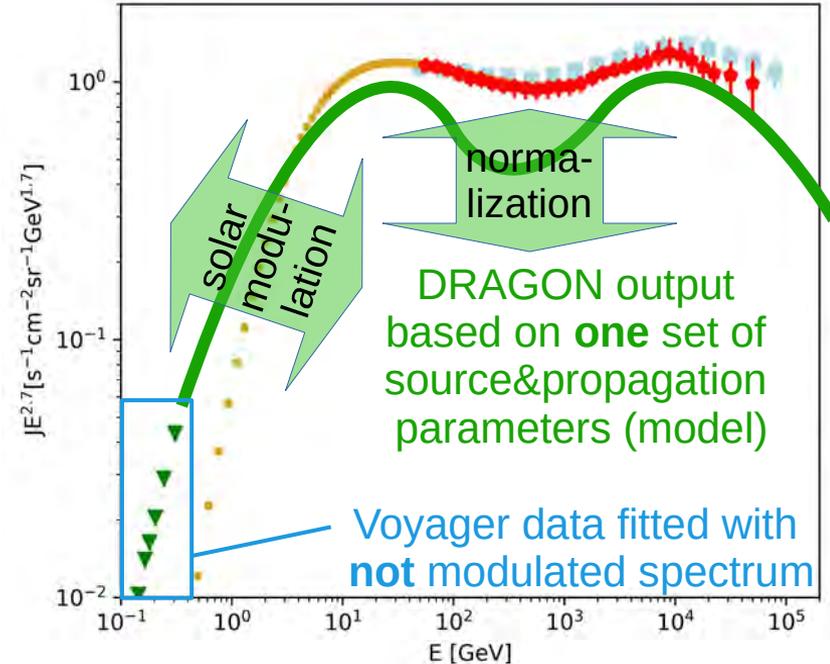
# Fitting the Spectra to the Data

- Parameters fitted by minimizing total  $\chi^2$  of all experimental data
  - Normalization correction factors
    - Proton
    - Helium
    - Carbon
    - Oxygen
  - Solar modulation potential parameters
    - $\Phi_0$
    - $\Phi_{1+}$  (positive charge)
    - $\Phi_{1-}$  (negative charge)
    - $R_0$

Charge sign and rigidity dependent solar modulation potential:

$$\Phi = \Phi_0 + \Phi_{1\pm} \left( \frac{1 + (R/R_0)^2}{((R/R_0)^3)} \right)$$

based on  
 Ilias Cholis, Dan Hooper, Tim Linden  
 Phys. Rev. D 93, 043016 (2016)  
 "A Predictive Analytic Model for the  
 Solar Modulation of Cosmic Rays"

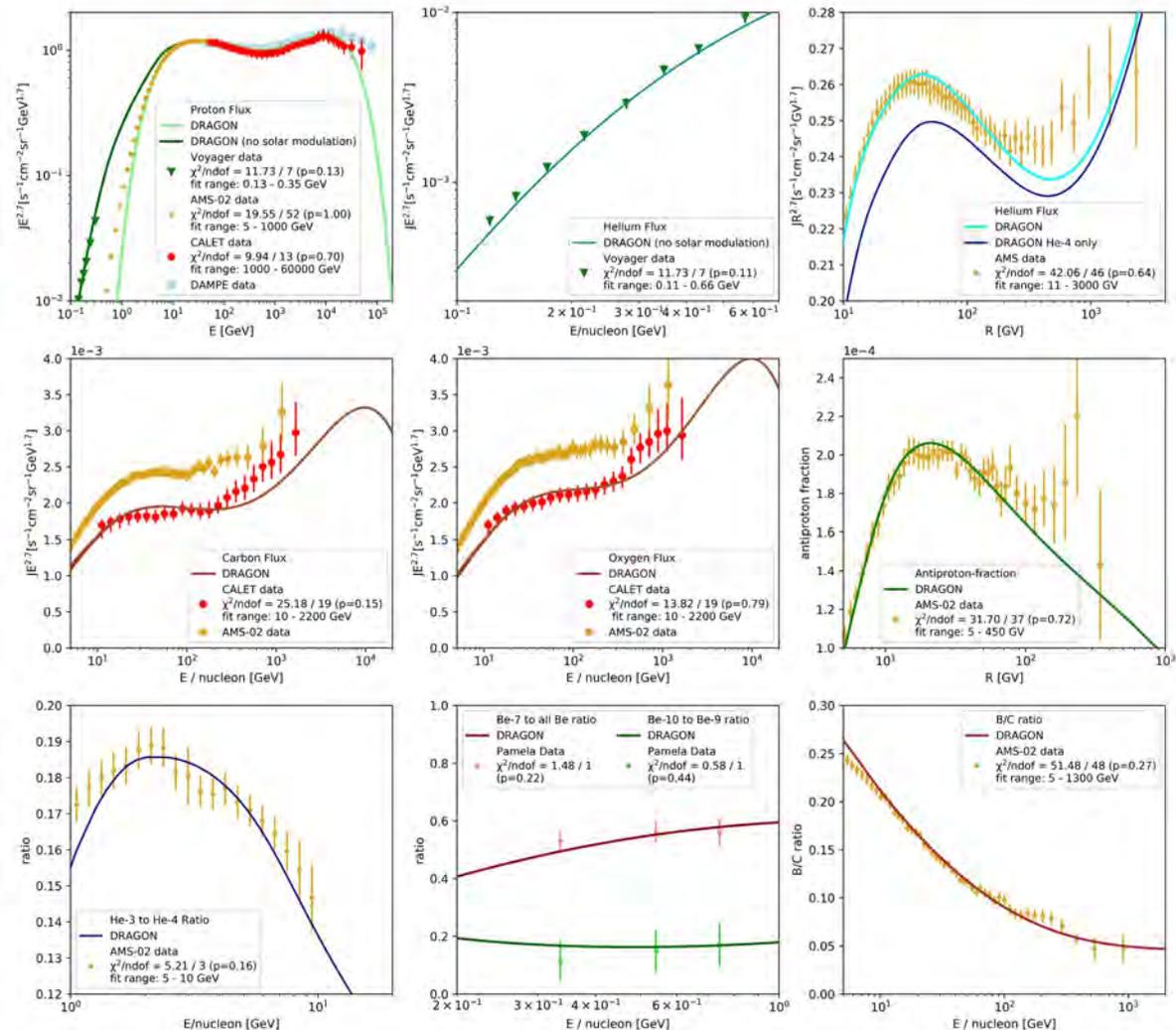


# Optimizing DRAGON Parameters

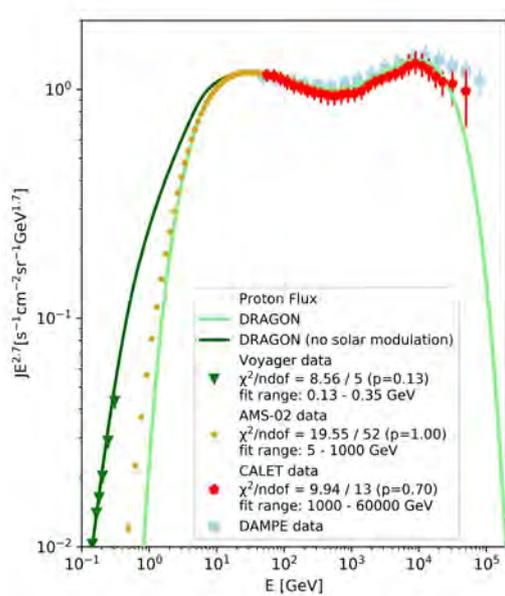
- Model quality parameters extracted from fit to data
  - Total  $\chi^2$  of all experimental data
  - Reduced  $\chi^2$  (single experiment), summed over experiments
  - Likelihood (p-value, single experiment), log-summed over experiments
  - Combinations of the above quality parameters  
(used in final step: log-sum of p-values, worst experiment doubled)
- Parameter space probed by “random” walk, combination of different methods used to select next model to calculate:
  - randomly within a given step size
  - following the negative gradient calculated from neighboring models
  - by interpolating/extrapolating parameters of already calculated models
- Initially optimization of helium-proton (with antiproton), and oxygen-beryllium separately, then combined by calculating silicon-proton and finally iron-proton (correction factor for influence of heavier nuclei used in partial calculations)

# Current Best-fit Model

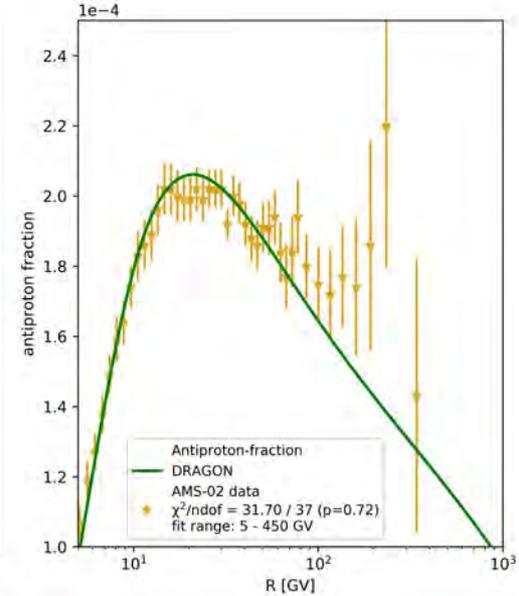
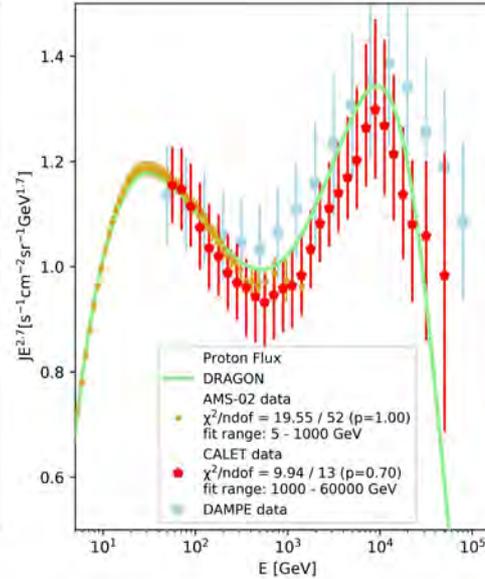
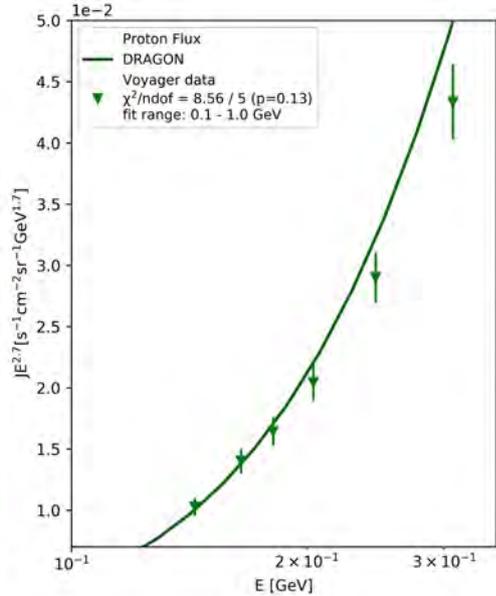
$\Upsilon_l$	$R_{bi}$	$S_{bi}$	$\Upsilon_h$	$R_{cut}$	$W_{sa}$
2.001	11.92 GV	0.213	2.345	27.91 TV	0.401 kpc
$D_0$	$r_s$	$z_s$	$\delta_l$	$R_{bl}$	$S_l$
$2.809 \times 10^{28}$ $\text{cm}^2/\text{s}$	9.84 kpc	4.20 kpc	0.246	7.732 GV	0.050
$\delta$	$R_{bh}$	$S_h$	$\delta_h$	$V_a$	total
0.504	911.8 GV	0.369	0.003	15.93 m/s	$\chi^2/\text{ndof}$ : 221/274



# Proton & Antiproton



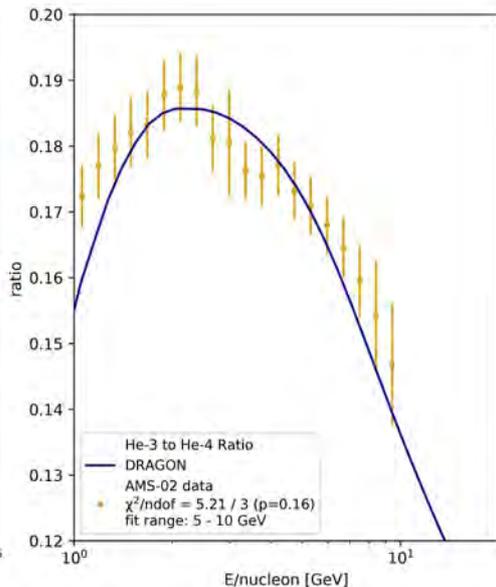
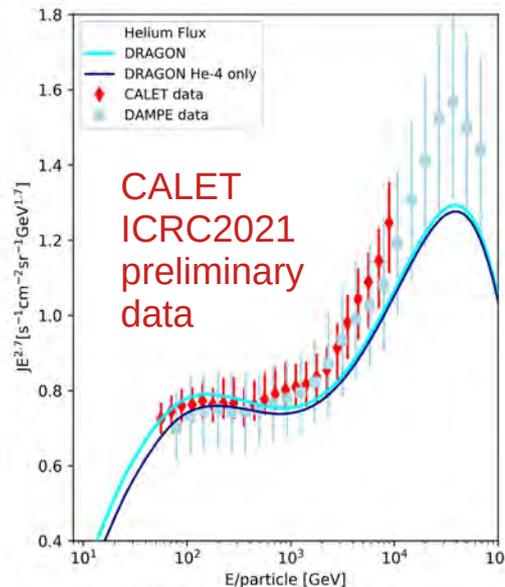
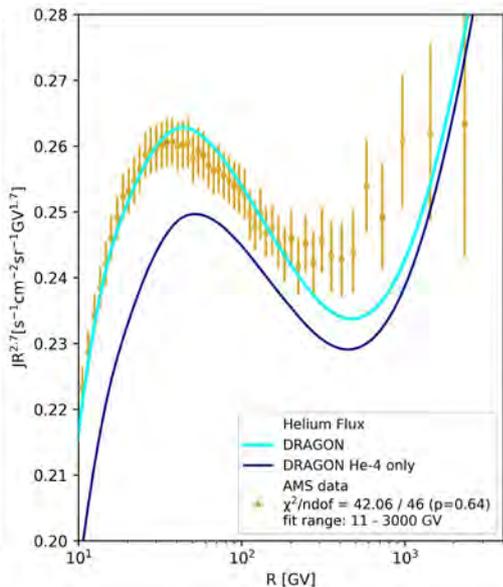
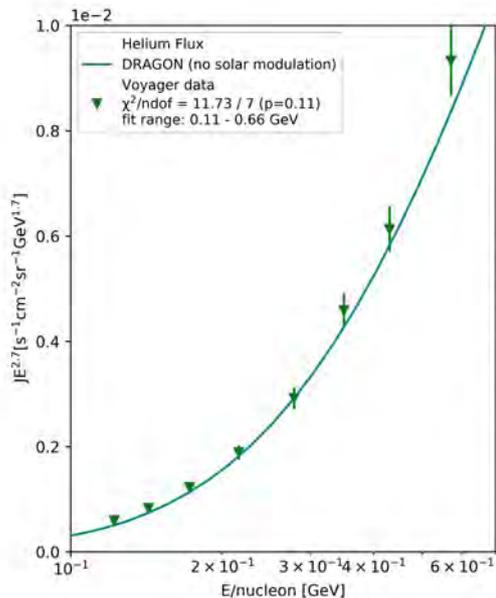
DAMPE proton:  
Sci.Adv. 5 (2019) 9



The exponential cut-off of the source spectrum at  $\sim 28$  TV well reproduces the sudden softening of the CALET proton data

AP “excess” above 100 GV visible by eye but not significant ( $\chi^2 / \text{ndof} < 1$ )

# Helium

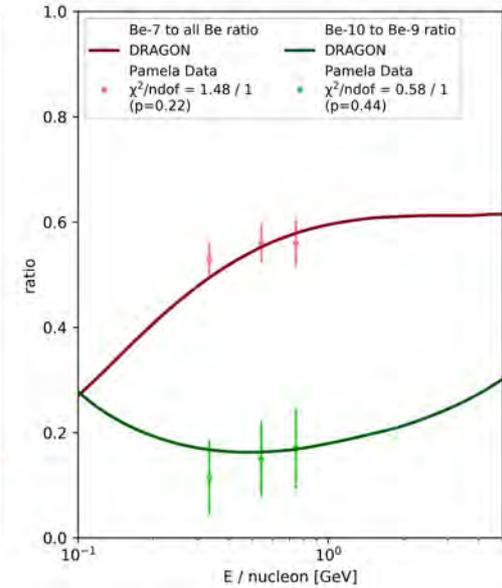
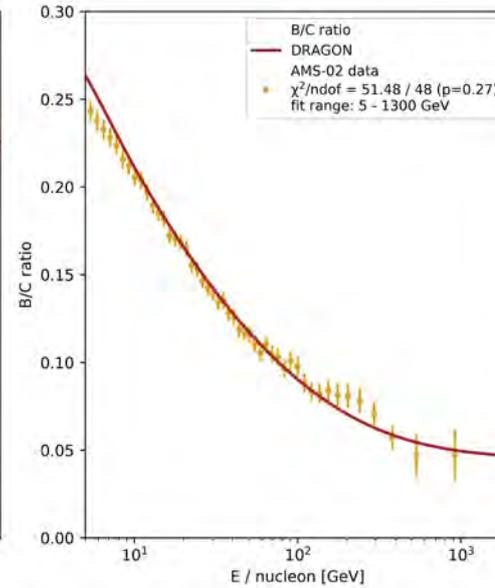
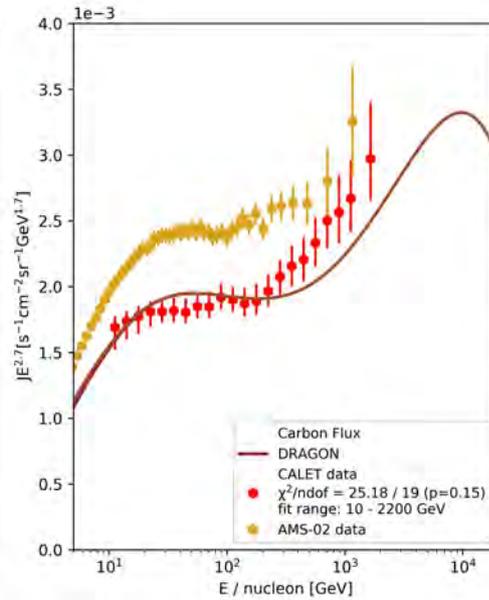
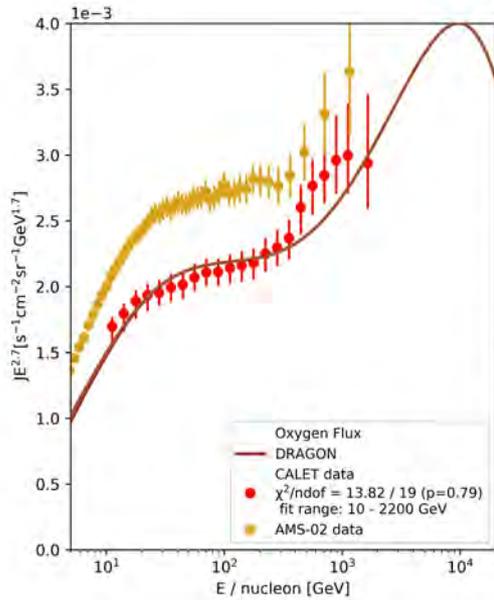


Secondary He-3 contributes significantly to the He spectrum  
 → influence of propagation conditions on spectral shape

CALET/DAMPE helium data not used in fitting, but in general agreement

DAMPE helium:  
 PRL 126, 201102 (2021)  
 CALET helium:  
 PoS ICRC2021 (2021) 101

# Oxygen, Carbon, Boron, Beryllium



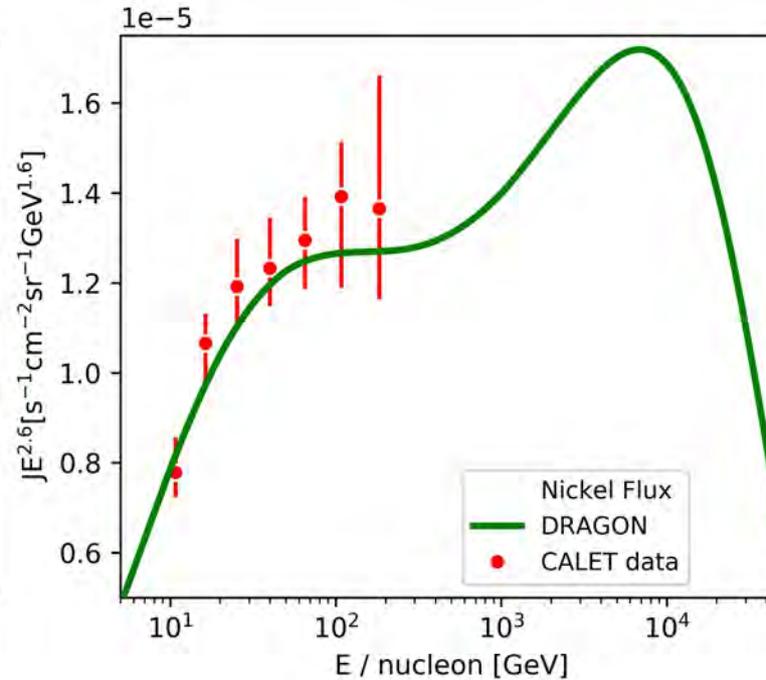
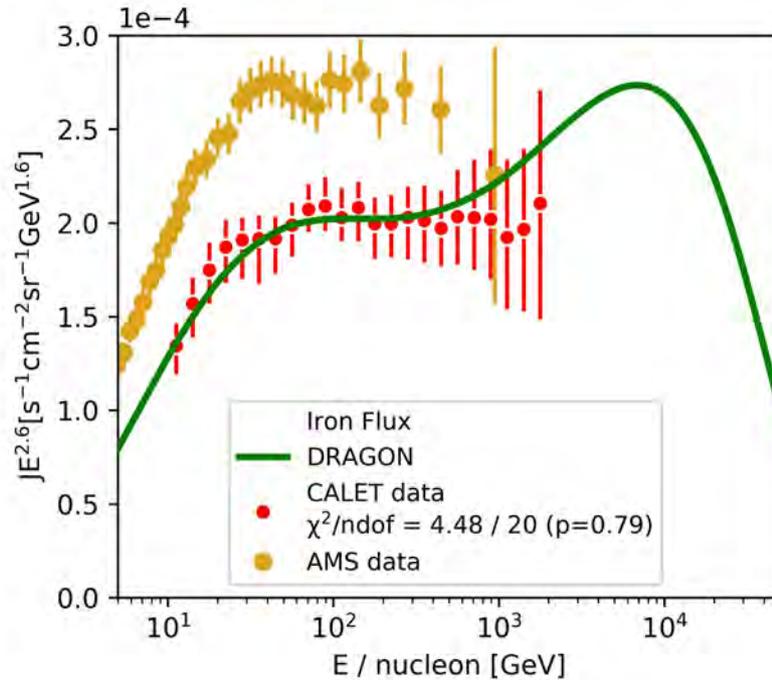
Normalization difference for C and O spectra between AMS-02 and CALET but general shape matches both datasets in general

AMS-02 C and O:  
PRL 119, 251101 (2017)

Model predicts B/C ratio to become flat in the TeV region

Exponential increase of the diffusion coefficient with  $z$  reproduces ratios of instable beryllium isotopes – correct effective diffusion zone height

# Iron, Nickel



Iron & nickel not used to optimize DRAGON parameters,  
separate normalization factor for iron fitted afterwards.  
Very good agreement with CALET data.

CALET iron:  
PRL 126, 241101 (2021)  
CALET nickel:  
PRL 128, 131103 (2022)  
AMS-02 iron:  
PRL 126, 041104 (2021)

# Conclusions / Outlook

- The presented model with a common source spectrum for all primary nuclei shows that explaining the current nuclei measurement data within experimental uncertainty based on propagation effects is possible.
- Differences in the spectral structures depending on the nuclei species could be caused by the propagation throughout the galactic halo with a diffusion coefficient which depends on both position and momentum.
- The presented model is the current best fit from the parameter space scan – further optimization is ongoing and new experimental data will be added.
- These detailed propagation conditions represent a huge parameter space which cannot easily be scanned to find allowed regions due to the time/resource requirements of the numerical calculation – preselection of models by machine learning algorithms might improve efficiency – future work.

**This work is supported by JSPS KAKENHI Grants No. JP21H05463 and No. JP21K03604**